## Section 8.3: Measures of Dispersion

Suppose you need a new quarterback for your football team and you are trying to decide between two quarterbacks who have played in the same league last season with roughly the same strength of schedule. The number of completions in each game for the 16 games of the previous season are shown for each quarterback:

| Game | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Quarterback A: | 27 | 30 | 32 | 28 | 33 | 28 | 29 | 30 | 25 | 24 | 19 | 22 | 37 | 27 | 32 | 25 |
| Quarterback B: | 25 | 33 | 40 | 19 | 39 | 35 | 17 | 12 | 32 | 33 | 12 | 39 | 30 | 17 | 35 | 30 |

Both Quarterbacks have the same average number of completions over the last season, $\mu=28$. However we see that Quarterback B has a a more varied performance record than Quarterback A. Obviously one needs to take this variability in the data into account when comparing the quarterbacks.

## Measures of Variability

The Range of a set of data is the largest measurement minus the smallest measurement.
Example Calculate the range for the data for Quarterback A and Quarterback B in the example above.
The minimum number of completions for Quarterback A is 19 , the maximum is 37 . The minimum number of completions for Quarterback B is 12 , the maximum is 40 . Hence the ranges are 18 for Quarterback A and 28 for Quarterback B.

Although the range is easy to compute it is a crude measure of variability. Consider the following two sets of data which have the same mean, 25 , and the same range, 10 , but obvious differences in the pattern of variability: (In the pictorial representation of the data shown below, we use an $\times$ above a data point to indicate a single observation of that data point in the sample)

| x | x |  |  |  |  |  |  |  | x | x |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| x | x | x |  |  |  |  |  | x | x | x |
| x | x | x | x | x | x | x | x | x | x | x |
| 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |

Data Set 1


Data Set 2

Data set 1 has most of its values far from the mean and is u-shaped, while data set 2 has most of its values closer to the mean and is mound shaped or bell shaped. In order to catch the different patterns in variability above, we need a more subtle measure than the range. Two widely used measure of consistency (or lack of it) in the data are given by the variance and the standard deviation. The formula for each depends on whether one is dealing with data from a population or a sample.

Population Variance and standard deviation: For a set of data $\left\{x_{1}, x_{2}, \ldots x_{n}\right\}$ for a population of size $n$, we define the population variance, denoted by $\sigma^{2}$, to be the average squared distance from the mean, $\mu$ :

$$
\sigma^{2}=\frac{\left(x_{1}-\mu\right)^{2}+\left(x_{2}-\mu\right)^{2}+\cdots+\left(x_{n}-\mu\right)^{2}}{n}
$$

(Note calculating the average distance from the mean requires using absolute values).

As with the calculation of the mean, we can shorten calculations if we have a frequency distribution at our disposal. For a set of data for a population of size $n$, with observed values $\left\{O_{1}, O_{2}, \ldots, O_{m}\right\}$ and frequencies $\left\{f_{1}, f_{2}, \ldots, f_{m}\right\}$ respectively, the population variance is given by :

$$
\sigma^{2}=\left(O_{1}-\mu\right)^{2} \frac{f_{1}}{n}+\left(O_{2}-\mu\right)^{2} \frac{f_{2}}{n}+\cdots+\left(O_{m}-\mu\right)^{2} \frac{f_{m}}{n}
$$

| Observations | Deviation | Squared Deviation | Sq. Dev. $\times$ Rel. Freq. |
| :---: | :---: | :---: | :---: |
| $O_{i}$ | $O_{i}-\mu$ | $\left(O_{i}-\mu\right)^{2}$ | $\left(O_{i}-\mu\right)^{2} \frac{f_{i}}{n}$ |
| $O_{1}$ | $O_{1}-\mu$ | $\left(O_{1}-\mu\right)^{2}$ | $\left(O_{1}-\mu\right)^{2} \frac{f_{1}}{n}$ |
| $O_{2}$ | $O_{2}-\mu$ | $\left(O_{2}-\mu\right)^{2}$ | $\left(O_{2}-\mu\right)^{2} \frac{f_{2}}{n}$ |
| $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ |
| $O_{m}$ | $O_{m}-\mu$ | $\left(O_{m}-\mu\right)^{2}$ | $\left(O_{m}-\mu\right)^{2} \frac{f_{m}}{n}$ |
|  |  |  | $\sigma^{2}=$ Sum |

Population Standard Deviation: The population standard deviation for the data is the square root of the population variance,

$$
\sigma=\sqrt{\sigma^{2}}
$$

Example 1: Find the variance, $\sigma^{2}$ and standard deviation, $\sqrt{\sigma^{2}}$, for the number of completions for each Quarterback above. The value of $\mu$ is 28 for both players.

Quarterback A

| $O_{i}$ <br> \# Completions | $f_{i}$ <br> Frequency |
| :---: | :---: |
| 19 | 1 |
| 22 | 1 |
| 24 | 1 |
| 25 | 2 |
| 27 | 2 |
| 28 | 2 |
| 29 | 1 |
| 30 | 2 |
| 32 | 2 |
| 33 | 1 |
| 37 | 1 |

Quarterback B

| $O_{i}$ <br> \# Completions | $f_{i}$ <br> Frequency |
| :---: | :---: |
| 12 | 2 |
| 17 | 2 |
| 19 | 1 |
| 25 | 1 |
| 30 | 2 |
| 32 | 1 |
| 33 | 2 |
| 35 | 2 |
| 39 | 2 |
| 40 | 1 |

## Quarterback A:

| Observations | Deviation | Squared Deviation | Sq. Dev. $\times$ Rel. Freq. |
| :---: | :---: | :---: | :---: |
| $O_{i}$ | $O_{i}-28$ | $\left(O_{i}-28\right)^{2}$ | $\left(O_{i}-28\right)^{\frac{f_{i}}{16}}$ |
| 19 | -9 | 81 | $\frac{81 \cdot 1}{16}$ |
| 22 | -6 | 36 | $\frac{36 \cdot 1}{16}$ |
| 24 | -4 | 16 | $\frac{16 \cdot 1}{16}$ |
| 25 | -3 | 9 | $\frac{9 \cdot 2}{16}$ |
| 27 | -1 | 1 | $\frac{1 \cdot 2}{16}$ |
| 28 | 0 | 0 | $\frac{0 \cdot 2}{16}$ |
| 29 | 1 | 1 | $\frac{1 \cdot 1}{16}$ |
| 30 | 2 | 4 | $\frac{4 \cdot 2}{16}$ |
| 32 | 4 | 16 | $\frac{16 \cdot 2}{16}$ |
| 33 | 5 | 25 | $\frac{25 \cdot 1}{16}$ |
| 37 | 9 | 81 | $\frac{81 \cdot 1}{16}$ |
|  |  |  | $\sigma^{2}=$ Sum |

Quarterback A: $\quad \sigma^{2}=\frac{300}{16}=\frac{75}{4}=18.75 \quad \sigma \approx 4.3301270189$

## Quarterback B:

| Observations | Deviation | Squared Deviation | Sq. Dev. $\times$ Rel. Freq. |
| :---: | :---: | :---: | :---: |
| $O_{i}$ | $O_{i}-28$ | $\left(O_{i}-28\right)^{2}$ | $\left(O_{i}-28\right)^{2} \frac{f_{i}}{16}$ |
| 12 | -16 | 256 | $\frac{256 \cdot 2}{16}$ |
| 17 | 11 | 121 | $\frac{121 \cdot 2}{16}$ |
| 19 | -9 | 81 | $\frac{81 \cdot 1}{16}$ |
| 25 | -3 | 9 | $\frac{9 \cdot 1}{16}$ |
| 30 | 2 | 4 | $\frac{4 \cdot 2}{16}$ |
| 32 | 4 | 16 | $\frac{16 \cdot 1}{16}$ |
| 33 | 5 | 25 | $\frac{25 \cdot 2}{16}$ |
| 35 | 7 | 49 | $\frac{49 \cdot 2}{16}$ |
| 39 | 11 | 121 | $\frac{121 \cdot 2}{16}$ |
| 40 | 12 | 144 | $\frac{144 \cdot 1}{16}$ |
|  |  |  | $\sigma^{2}=$ Sum |

Quarterback B: $\quad \sigma^{2}=\frac{1402}{16}=87.625 \quad \sigma=9.3608226134$

Sample Variance and Standard Deviation : If we calculate the variance according to the formula given above, for a sample from a particular population, it is not accurate (biased) as an estimate for the population variance. So for a sample from a given population, we use the sample variance as an unbiased estimator of the population variance.

Given a sample, $\left\{x_{1}, \quad x_{2}, \quad \ldots \quad x_{n}\right\}$, of size $n$ from a population, where the sample mean is given by $\bar{x}$, the sample variance is given by

$$
s^{2}=\frac{\left(x_{1}-\bar{x}\right)^{2}+\left(x_{2}-\bar{x}\right)^{2}+\cdots+\left(x_{n}-\bar{x}\right)^{2}}{n-1}
$$

The sample standard deviation is given by

$$
s=\sqrt{s^{2}}
$$

If the data is given in a frequency distribution, we can shorten the calculations. If the outcomes in the sample are given by $\left\{O_{1}, O_{2}, \ldots, O_{m}\right\}$ with respective frequencies given by $\left\{f_{1}, f_{2}, \ldots, f_{m}\right\}$, then

$$
s^{2}=\frac{\left(O_{1}-\bar{x}\right)^{2} f_{1}+\left(O_{2}-\bar{x}\right)^{2} f_{2}+\cdots+\left(O_{n}-\bar{x}\right)^{2} f_{m}}{n-1}
$$

Example 3 A random sample of size twenty of a golfer's scores for nine-hole rounds of golf over the past year are as follows:

$$
\begin{gathered}
39,40,40,41, \quad 39,40,44,43,40,41,40,41,, 41, \\
42,43,40,41,41,41,43 .
\end{gathered}
$$

Compute the mean, sample variance and the sample standard deviation for the sample of the golfer's scores. You can view the sample variance as an estimate of the overall variance of the golfer's scores. The mean is 41 .

| Observations | Frequency | Deviation | Squared Deviation | Sq. Dev. $\times$ Rel. Freq. |
| :---: | :---: | :---: | :---: | :---: |
| $O_{i}$ | $f_{i}$ | $O_{i}-28$ | $\left(O_{i}-28\right)^{2}$ | $\left(O_{i}-28\right)^{2} \cdot f_{i}$ |
| 39 | 2 | -2 | 4 | 8 |
| 40 | 6 | -1 | 1 | 6 |
| 41 | 7 | 0 | 0 | 0 |
| 42 | 1 | 1 | 1 | 1 |
| 43 | 3 | 2 | 4 | 12 |
| 44 | 1 | 3 | 9 | 9 |
| Sample size $=$ | 20 |  | Sum $=$ | 36 |

Hence $s^{2}=\frac{36}{20-1}=\frac{36}{19} \approx 1.8947368421 . \quad s \approx 1.3764944032$.
As long as we're up, the median is also 41 and the mode is 41 as well.
You can compute the mean from the frequency table. Start adding frequencies from either the t or bottom until you get to 10 . Since 10 is even average the 10 th and the 11th entries. From the botto in this example, $1+3+1=5$ and $1+3+1+7=12$ so the 10 th and the 11 th entries are both vskip .1in Working from the top, $2+6=8$ and $2+6+7=15$ so both the 10 th and the 11 th entries are 41 .

## Interpreting The Standard Deviation

When presented with raw scores for performance, it is difficult to interpret their meaning without some measure of center and variability for the population from which they come. In any set of data, whether it is population data or a sample, observations that are more than 3 standard deviations from the mean are rare and exceptional. One such rule demonstrating this is the empirical rule for mound shaped data shown below. We will explore this rule in more detail when we study the normal distribution.

## The Empirical Rule for Mound Shaped Data

The empirical rule given below applies to data sets with frequency distributions that are mound shaped and symmetric, like the one shown below.


Empirical Rule If the data has a frequency distribution which is mound shaped and symmetric, we have the following empirical rule:

- Approximately $68 \%$ of the measurements will fall within 1 standard deviation of the mean i.e. within the interval $(\bar{x}-s, \bar{x}+s)$ for a sample and $(\mu-\sigma, \mu+\sigma)$ for a population.
- Approximately $95 \%$ of the measurements will fall within 2 standard deviations of the mean, i.e. within the interval $(\bar{x}-2 s, \bar{x}+2 s)$ for samples and $(\mu-2 \sigma, \mu+2 \sigma)$ for a population.
- Approximately $99.7 \%$ of the measurements(essentially all) will fall within 3 standard deviations of the mean, i.e. within the interval $(\bar{x}-3 s, \bar{x}+3 s)$ for samples and $(\mu-3 \sigma, \mu+3 \sigma)$ for a population.

Mound shaped distributions are very important because they frequently occur as population distributions. Even more importantly, the central limit theorem says that if we take all samples of a given size from a population and calculate all of the means, then the distribution of the means is mound shaped (Normal). We will study Normal distributions in more detail later.

## Numerical Measures of Relative Standing

Quite often when interpreting a data observation, such as a baby's height and weight, we are interested in how it compares to the rest of the relevant population. Measures of relative standing describe the location of a particular measurement relative to the rest of the data. We explore some of the standard measures of relative standing below.

Z-Scores The z-score for a particular measurement in a set of data, measures how many standard deviations that measurement lies away from the mean.

Definition The sample z-score for a measurement x in a set of data is

$$
z=\frac{x-\bar{x}}{s} .
$$

The population z -score for a data measurement, x , is

$$
z=\frac{x-\mu}{\sigma}
$$

Example The scores on the LSAT for a particular year have a mound shaped distribution. The mean is $\mu=150$ and the standard deviation is $\sigma=10$. The distribution is shown below.

(a) Use the empirical rule to determine what percentage of prospective law students have z scores between - 2 and 2 .

From the formula, $x=\mu+z \cdot \sigma$ so a z score between -2 and 2 means you are in the interval ( $\mu-2 \sigma, \mu+2 \sigma$ ) and hence by the Empirical Rule $95 \%$ of the students taking the exam have z scores between -2 and 2 .
(b) If you scored 175 on the exam, what would your z-score be?

From the formula, $z=\frac{x-\mu}{\sigma}=\frac{175-150}{10}=2.5$.

Example In 2013 Mary was among the college bound seniors who took the SAT and ACT exams. Her composite score on the SAT was 2500 and her composite score on the ACT was 34 . The national average for the composite score on the SAT among college bound seniors for that year was 1499 and the standard deviation was 319. The national average for the ACT among college bound seniors for that year was 22.5 and the standard deviation was 4.9.
Find Mary's z-score for both exams and use the z-scores to compare Mary's performance on both exams.

$$
\begin{aligned}
& z_{\mathrm{SAT}}=\frac{x-\mu}{\sigma}=\frac{2500-1499}{319} \approx 3.1379310345 \\
& \quad z_{\mathrm{ACT}}=\frac{x-\mu}{\sigma}=\frac{34-22.5}{4.9} \approx 2.3469387755
\end{aligned}
$$

Mary did better on the SAT.

Rank We can also use rank to measure relative standing, by ranking the data as 1st, 2nd, 3rd, according to the size of the data measurement. This is commonly used in racing, where a lower time leads to a higher position, also in many competitions a higher number of points or wins leads to a higher rank. When two data measurements are the same (a tie) we can give both the same rank and skip a rank. A closely related measure of relative standing is given by the percentile:

## Percentiles

Recall that the median of a set of data is number for which $50 \%$ of the measurements lie at or below the median and $50 \%$ lie at or above it. This is the 50 th percentile of the distribution.

For any set of $n$ measurements, (arranged in ascending or descending order), the $p$ th percentile is a number such that $p \%$ of the measurements fall at or below that number and $(100-p) \%$ of the measurements fall above it. The calculation of percentiles is not well defined and there are a few conventions which one might adopt for choosing a value for a percentile. We will adopt a relatively simple convention which mostly agrees with our calculation of the median from before. (If the sample size is odd, it agrees precisely and if the sample size is even it is close.) For a set of data of size $N$, to calculate the $P$-th percentile we order our data from smallest to largest and choose the $n$-th data point on the list, where $n$ is the nearest integer above (or equal to) $\frac{P}{100} \times N$.
Example 1 Find the 10th percentile, the 25 th percentile, the 50 th percentile, the 75 th percentile and the 90 th percentile of the following set of 20 exam scores:
$60,71, ~ 85, ~ 99, ~ 100, ~ 76, ~ 98, ~ 61, ~ 75, ~ 82, ~ 95, ~ 72, ~ 88, ~ 61, ~ 72, ~ 80, ~ 100, ~ 90, ~ 60, ~ 70 . ~$
IMPORTANT POINT: the percentiles only depend on the number of data points, NOT on the data, except for order.

In this example there are 20 data points and in increasing order they are

$$
60,60,61,61,70,71,72,72,75,76,80,82,85,88,90,95,98,99,100,100
$$

For the $10^{\text {th }}$ percentile, $\frac{P}{100} \cdot N=\frac{10}{100} \cdot 20=2$. Hence 60 is the answer.
For the $25^{\text {th }}$ percentile, $\frac{P}{100} \cdot N=\frac{25}{100} \cdot 20=5$. Hence 70 is the answer.
For the $50^{\text {th }}$ percentile, $\frac{P}{100} \cdot N=\frac{50}{100} \cdot 20=10$. Hence 76 is the answer. Notice the $50^{\text {th }}$ percentile is not quite the median, which in this case is $\frac{76+80}{2}=78$. For the $75^{\text {th }}$ percentile, $\frac{P}{100} \cdot N=\frac{75}{100} \cdot 20=15$. Hence 90 is the answer. For the $90^{\text {th }}$ percentile, $\frac{P}{100} \cdot N=\frac{90}{100} \cdot 20=18$. Hence 100 is the answer.

Just to have an example where the relevant calculation is not an integer, for the $37^{\text {th }}$ percentile, $\frac{P}{100} \cdot N=\frac{37}{100} \cdot 20=7.4$. Hence we want the $8^{\text {th }}$ number on the list or 72.

Example Attached you will find list of the top forty players from the NBA with the number of rebounds for the 2013-2014 regular season for each given in the highlighted column. The players are ranked 1-40 according to the number of rebounds.

What is the 95 -th percentile for the number of rebounds among all NBA players for the 2013-2014 regular season.

There are 40 data points so $\frac{P}{100} \cdot N=\frac{95}{100} \cdot 40=38$. Hence we need to count 38 rows starting at the bottom. For large numbers like this it would be easier to count from the top. The formula is $40-38+1=3$ so the answer is 963 . The +1 comes from the fact that we start counting with 1 .

| Rebounds Leaders - All Players |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| RK | PLAYER | TEAM | GP | MPG | OFF | ORPG | DEF | DRPG | REB | RPG | RP48 |
| 1 | DeAndre Jordan, C | LAC | 82 | 35.0 | 331 | 4.0 | 783 | 9.5 | 1114 | 13.6 | 18.6 |
| 2 | Andre Drummond, C | DET | 81 | 32.3 | 440 | 5.4 | 631 | 7.8 | 1071 | 13.2 | 19.6 |
| 3 | Kevin Love, PF | MIN | 77 | 36.3 | 224 | 2.9 | 739 | 9.6 | 963 | 12.5 | 16.5 |
| 4 | Joakim Noah, C | CHI | 80 | 35.3 | 282 | 3.5 | 618 | 7.7 | 900 | 11.3 | 15.3 |
| 5 | Dwight Howard, C | HOU | 71 | 33.7 | 231 | 3.3 | 635 | 8.9 | 866 | 12.2 | 17.3 |
| 6 | DeMarcus Cousins, C | SAC | 71 | 32.4 | 218 | 3.1 | 613 | 8.6 | 831 | 11.7 | 17.4 |
| 7 | Zach Randolph, PF | MEM | 79 | 34.2 | 265 | 3.4 | 530 | 6.7 | 795 | 10.1 | 14.1 |
| 8 | Al Jefferson, C | CHA | 73 | 35.0 | 156 | 2.1 | 636 | 8.7 | 792 | 10.8 | 14.9 |
| 9 | Marcin Gortat, C | WSH | 81 | 32.8 | 202 | 2.5 | 565 | 7.0 | 767 | 9.5 | 13.9 |
| 10 | LaMarcus Aldridge, PF | POR | 69 | 36.2 | 166 | 2.4 | 600 | 8.7 | 766 | 11.1 | 14.7 |
| RK | PLAYER | team | GP | MPG | OFF | ORPG | DEF | DRPG | REB | RPG | RP48 |
| 11 | Greg Monroe, PF | DET | 82 | 32.8 | 256 | 3.1 | 504 | 6.1 | 760 | 9.3 | 13.6 |
| 12 | Blake Griffin, PF | LAC | 80 | 35.8 | 192 | 2.4 | 565 | 7.1 | 757 | 9.5 | 12.7 |
| 13 | Tristan Thompson, PF | CLE | 82 | 31.6 | 269 | 3.3 | 485 | 5.9 | 754 | 9.2 | 14.0 |
| 14 | Tim Duncan, PF | SA | 74 | 29.2 | 158 | 2.1 | 563 | 7.6 | 721 | 9.7 | 16.0 |
| 15 | Jonas Valanciunas, C | TOR | 81 | 28.2 | 226 | 2.8 | 488 | 6.0 | 714 | 8.8 | 15.0 |
| 16 | Serge Ibaka, PF | OKC | 81 | 32.9 | 224 | 2.8 | 485 | 6.0 | 709 | 8.8 | 12.8 |
| 17 | Robin Lopez, C | POR | 82 | 31.8 | 326 | 4.0 | 373 | 4.5 | 699 | 8.5 | 12.9 |
| 18 | Kenneth Faried, PF | DEN | 80 | 27.2 | 238 | 3.0 | 446 | 5.6 | 684 | 8.6 | 15.1 |
| 19 | Anthony Davis, PF | NO | 67 | 35.2 | 207 | 3.1 | 466 | 7.0 | 673 | 10.0 | 13.7 |
| 20 | Andrew Bogut, C | GS | 67 | 26.4 | 182 | 2.7 | 489 | 7.3 | 671 | 10.0 | 18.2 |
| RK | PLAYER | TEAM | GP | MPG | OFF | ORPG | DEF | DRPG | REB | RPG | RP48 |
| 21 | Spencer Hawes, PF | CLE/PHI | 80 | 30.9 | 131 | 1.6 | 529 | 6.6 | 660 | 8.3 | 12.8 |
| 22 | David Lee, PF | GS | 69 | 33.2 | 182 | 2.6 | 461 | 6.7 | 643 | 9.3 | 13.5 |
| 23 | Derrick Favors, C | UTAH | 73 | 30.2 | 199 | 2.7 | 438 | 6.0 | 637 | 8.7 | 13.9 |
| 24 | J.J. Hickson, C | DEN | 69 | 26.9 | 206 | 3.0 | 426 | 6.2 | 632 | 9.2 | 16.3 |
|  | Carlos Boozer, PF | CHI | 76 | 28.2 | 137 | 1.8 | 495 | 6.5 | 632 | 8.3 | 14.2 |
| 26 | Anderson Varejao, C | CLE | 65 | 27.7 | 187 | 2.9 | 442 | 6.8 | 629 | 9.7 | 16.8 |
| 27 | Paul Millsap, PF | ATL | 74 | 33.5 | 154 | 2.1 | 473 | 6.4 | 627 | 8.5 | 12.1 |
| 28 | Nikola Vucevic, C | ORL | 57 | 31.8 | 185 | 3.2 | 441 | 7.7 | 626 | 11.0 | 16.6 |
|  | Miles Plumlee, C | PHX | 80 | 24.6 | 198 | 2.5 | 428 | 5.4 | 626 | 7.8 | 15.3 |
| 30 | Carmelo Anthony, SF | NY | 77 | 38.7 | 145 | 1.9 | 477 | 6.2 | 622 | 8.1 | 10.0 |
| RK | PLAYER | TEAM | GP | MPG | OFF | ORPG | DEF | DRPG | REB | RPG | RP48 |
| 31 | Nicolas Batum, SF | POR | 82 | 36.0 | 116 | 1.4 | 495 | 6.0 | 611 | 7.5 | 9.9 |
| 32 | Jared Sullinger, C | BOS | 74 | 27.6 | 241 | 3.3 | 360 | 4.9 | 601 | 8.1 | 14.1 |
| 33 | Enes Kanter, C | UTAH | 80 | 26.7 | 222 | 2.8 | 376 | 4.7 | 598 | 7.5 | 13.4 |
|  | Kevin Durant, SF | OKC | 81 | 38.5 | 58 | 0.7 | 540 | 6.7 | 598 | 7.4 | 9.2 |
| 35 | Pau Gasol, PF | LAL | 60 | 31.4 | 124 | 2.1 | 456 | 7.6 | 580 | 9.7 | 14.8 |
| 36 | Lance Stephenson, SG | IND | 78 | 35.3 | 95 | 1.2 | 463 | 5.9 | 558 | 7.2 | 9.7 |
|  | Taj Gibson, PF | CHI | 82 | 28.7 | 200 | 2.4 | 358 | 4.4 | 558 | 6.8 | 11.4 |
| 38 | David West, PF | IND | 80 | 30.9 | 120 | 1.5 | 422 | 5.3 | 542 | 6.8 | 10.5 |
|  | Paul George, SF | IND | 80 | 36.2 | 64 | 0.8 | 478 | 6.0 | 542 | 6.8 | 9.0 |
| 40 | Samuel Dalembert, C | DAL | 80 | 20.2 | 200 | 2.5 | 341 | 4.3 | 541 | 6.8 | 16.1 |

